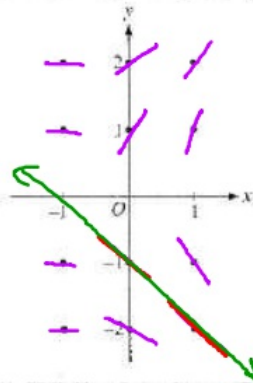


5. Consider the differential equation  $\frac{dy}{dx} = \frac{x+1}{y}$

a) On the axes provided, sketch a slope field for the given differential equation at the twelve points indicated and for  $-1 < x < 1$ , sketch the solution curve passing through the point  $(0, -1)$ .



b) While the slope field in part (a) is drawn at only twelve points, it is defined at every point in the  $xy$ -plane for which  $y \neq 0$ . Describe all

points in the  $xy$ -plane,  $y \neq 0$ , for which  $\frac{dy}{dx} = -1$

$$y = -|x - 1|$$

c) Find the particular solution  $y = f(x)$  to the given differential equation with the initial condition  $f(0) = -2$ .

~~$$\frac{dy}{dx} = \frac{x+1}{y} (dx)$$~~

$$(y) dy = \frac{(x+1)}{y} dx (y)$$

$$\int y dy = \int (x+1) dx$$

$$\frac{1}{2} y^2 = \frac{1}{2} x^2 + x + C$$

$$2 = C$$

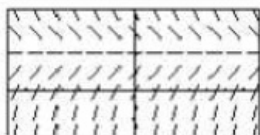
$$\frac{1}{2} y^2 = \frac{1}{2} x^2 + x + 2$$

$$y^2 = x^2 + 2x + 4$$

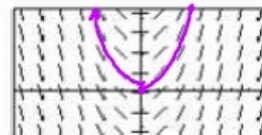
$$y = -\sqrt{x^2 + 2x + 4}$$

Match the following differential equation with the correct slope field

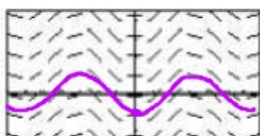
(A) #9



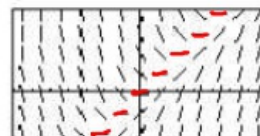
(B) #10



(C) #7



(D) #8



7.  $\frac{dy}{dx} = \sin x$

$y = -\cos x + C$

8.  $\frac{dy}{dx} = x - y$

$y = x$

$\frac{dy}{dx} = 0$

9.  $\frac{dy}{dx} = 2 - y$

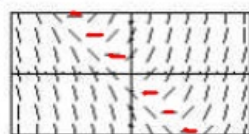
$y = 2$   $\frac{dy}{dx} = 0$

10.  $\frac{dy}{dx} = x$

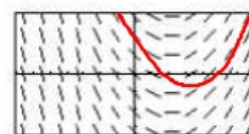
$y = \frac{1}{2}x^2 + C$

#14

(A)



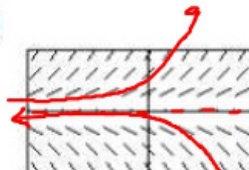
(B)



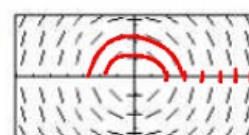
#11

#12

(C)



(D)



#13

11.  $\frac{dy}{dx} = 0.5x - 1$

$y = \text{Quadratic}$

12.  $\frac{dy}{dx} = 0.5y$

$\int \frac{dy}{y} = \int 0.5 dx$   
 $\ln y = 0.5x + C$   
 $y = e^{0.5x}$

13.  $\frac{dy}{dx} = -\frac{x}{y}$

$y \neq 0$

$\int y dy = \int -x dx$   
 $\frac{1}{2}y^2 = -\frac{1}{2}x^2 + C$   
 $y^2 = -x^2 + C$   
 $y = \pm \sqrt{-x^2 + C}$

14.  $\frac{dy}{dx} = x + y$

$\frac{dy}{dx} = 0$

$y$  and  $x$  opp.

Rewrite each definite integral in terms of u and du

1.  $\int_{x=0}^{x=1} (5x+4)^5 dx$  Let  $u = 5x + 4$

$$\int_4^9 u^5 dx$$

$$\frac{du}{dx} = 5$$

$$du = 5 dx$$

$$\frac{du}{5} = dx$$

$$\int_4^9 u^5 \frac{du}{5}$$

$$\int_4^9 \frac{1}{5} u^5 du$$

2.  $\int_0^2 3x^2(x^3+4)^5 dx$  Let  $u = x^3 + 4$

$$\int_4^{12} (3x^2)(u)^5 dx$$

$$\left(\frac{du}{dx}\right) = 3x^2$$

$$\int_4^{12} \left(\frac{du}{dx}\right) u^5 dx$$

$$\int_4^{12} u^5 du$$

$$3. \int_1^3 \cos(2x+1) dx \text{ Let } u = 2x+1 \rightarrow \frac{du}{dx} = 2$$

$$\int_3^7 \cos(u) dx$$

$$\frac{du}{2} = dx$$

$$\int_3^7 \cos(u) \frac{du}{2} = \int_3^7 \frac{1}{2} \cos(u) du = \frac{1}{2} \int_3^7 \cos(u) du$$

$$4. \int_0^{\pi/4} \frac{\sin x}{(\cos x)^5} dx \text{ Let } u = \cos x \quad \frac{du}{dx} = -\sin x$$

$$\int_1^{\sqrt{2}/2} \frac{\sin x}{u^5} dx$$

$$\frac{du}{-\sin x} = dx$$

$$\int_1^{\sqrt{2}/2} \frac{\sin x}{u^5} \cdot \frac{du}{-\sin x} = \int_1^{\sqrt{2}/2} \frac{-1}{u^5} du = \int_1^{\sqrt{2}/2} -u^{-5} du$$

$$= \int -\frac{du}{u^5}$$